

**Section A - Answers**

- |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 1 | D | 2 | A | 3 | B | 4 | C |
| 5 | D | 6 | B | 7 | B | 8 | D |

**2 marks each (16 marks)**

**Section B - Marking Scheme**

	Give 1 mark for each •	Illustration(s) for awarding each mark
9(a)	<p>ans: (11, -10, 2) (2 marks)</p> <ul style="list-style-type: none"> <li>•<sup>1</sup> valid method</li> <li>•<sup>2</sup> answer</li> </ul>	<ul style="list-style-type: none"> <li>•<sup>1</sup> evidence of using stepping out/section formula</li> <li>•<sup>2</sup> (11, -10, 2)</li> </ul>
(b)	<p>ans: proof (4 marks)</p> <ul style="list-style-type: none"> <li>•<sup>1</sup> finds <math>\vec{DA}</math></li> <li>•<sup>2</sup> finds <math>\vec{DC}</math></li> <li>•<sup>3</sup> finds <math>\vec{DA} \cdot \vec{DC}</math></li> <li>•<sup>4</sup> conclusion</li> </ul>	<ul style="list-style-type: none"> <li>•<sup>1</sup> <math>\vec{DA} = \begin{pmatrix} -10 \\ 10 \\ -5 \end{pmatrix}</math></li> <li>•<sup>2</sup> <math>\vec{DC} = \begin{pmatrix} -7 \\ -6 \\ 2 \end{pmatrix}</math></li> <li>•<sup>3</sup> <math>\vec{DA} \cdot \vec{DC} = 70 - 60 - 10 = 0</math></li> <li>•<sup>4</sup> since <math>\vec{DA} \cdot \vec{DC} = 0</math>; <math>\angle ADC</math> is right angled</li> </ul>
(c)	<p>ans: proof (3 marks)</p> <ul style="list-style-type: none"> <li>•<sup>1</sup> finds <math>\vec{BA}</math> and <math>\vec{BC}</math></li> <li>•<sup>2</sup> finds <math>\vec{BA} \cdot \vec{BC}</math></li> <li>•<sup>3</sup> conclusion</li> </ul>	<ul style="list-style-type: none"> <li>•<sup>1</sup> <math>\vec{BA} = \begin{pmatrix} -4 \\ 4 \\ -2 \end{pmatrix}</math>    <math>\vec{BC} = \begin{pmatrix} -1 \\ -12 \\ 5 \end{pmatrix}</math></li> <li>•<sup>2</sup> <math>\vec{BA} \cdot \vec{BC} = 4 - 48 - 10 = -54</math></li> <li>•<sup>3</sup> scalar product <math>&lt; 0</math> so obtuse angle</li> </ul>

	Give 1 mark for each •	Illustration(s) for awarding each mark	
10	<b>ans: proof (3 marks)</b> <ul style="list-style-type: none"> <li>•<sup>1</sup> applies given info to new function</li> <li>•<sup>2</sup> knows to substitute in function</li> <li>•<sup>3</sup> simplifies to required form</li> </ul>	<ul style="list-style-type: none"> <li>•<sup>1</sup> <math>\cos^2 \frac{1}{2}x^\circ = \frac{1}{2}(\cos x^\circ + 1)</math></li> <li>•<sup>2</sup> <math>6[\frac{1}{2}(\cos x^\circ + 1)] + \sqrt{3} \sin x^\circ</math></li> <li>•<sup>3</sup> <math>3(\cos x + 1)] + \sqrt{3} \sin x^\circ; 3\cos x + 3 + \sqrt{3} \sin x^\circ</math></li> </ul>	
	<b>ans: <math>\sqrt{12}\cos(x - 30)^\circ + 3</math> (3 marks)</b> <ul style="list-style-type: none"> <li>•<sup>1</sup> finds <math>k</math></li> <li>•<sup>2</sup> finds <math>\tan \alpha</math></li> <li>•<sup>3</sup> finds <math>\alpha</math></li> </ul>		<ul style="list-style-type: none"> <li>•<sup>1</sup> <math>k = \sqrt{9+3} = \sqrt{12}</math></li> <li>•<sup>2</sup> <math>\tan \alpha = \frac{\sqrt{3}}{3}</math></li> <li>•<sup>3</sup> <math>\alpha = 30^\circ</math></li> </ul>
	<b>ans: <math>240^\circ</math> (4 marks)</b> <ul style="list-style-type: none"> <li>•<sup>1</sup> equates to 0</li> <li>•<sup>2</sup> simplifies</li> <li>•<sup>3</sup> finds values</li> <li>•<sup>4</sup> discards</li> </ul>		<ul style="list-style-type: none"> <li>•<sup>1</sup> <math>\sqrt{12}\cos(x - 30)^\circ + 3 = 0</math></li> <li>•<sup>2</sup> <math>\cos(x - 30)^\circ = -\frac{3}{\sqrt{12}}</math></li> <li>•<sup>3</sup> <math>x = 240^\circ; 360^\circ</math></li> <li>•<sup>4</sup> <math>240^\circ</math></li> </ul>
11	<b>ans: <math>P = 4t^{1/2}</math> (3 marks)</b> <ul style="list-style-type: none"> <li>•<sup>1</sup> knows form of equation, takes logs, expands</li> <li>•<sup>2</sup> finds <math>b</math></li> <li>•<sup>3</sup> writes relationship</li> </ul>	<ul style="list-style-type: none"> <li>•<sup>1</sup> <math>y = ax^b; \log_2 P = \frac{1}{2} \log_2 t + 2</math></li> <li>•<sup>2</sup> <math>b = \frac{1}{2}; \log_2 a = 2; a = 2^2; a = 4</math></li> <li>•<sup>3</sup> <math>P = 4t^{1/2}</math></li> </ul>	
	<b>ans: proof (3 marks)</b> <ul style="list-style-type: none"> <li>•<sup>1</sup> subs into expression</li> <li>•<sup>2</sup> starts to simplify</li> <li>•<sup>3</sup> completes simplification to answer</li> </ul>		<ul style="list-style-type: none"> <li>•<sup>1</sup> <math>4t^{\frac{1}{2}} = \sqrt{8} + 4</math></li> <li>•<sup>2</sup> <math>t^{\frac{1}{2}} = \frac{1}{4}(\sqrt{8} + 4); t = [\frac{1}{4}(\sqrt{8} + 4)]^2</math></li> <li>•<sup>3</sup> <math>t = \frac{1}{16}(8 + 8\sqrt{8} + 16); t = \frac{1}{16}(24 + 16\sqrt{2})</math>  <math>t = \frac{24}{16} + \sqrt{2}; t = \frac{3}{2} + \frac{2\sqrt{2}}{2}; t = \frac{1}{2}(3 + 2\sqrt{2})</math></li> </ul>
12	<b>ans: <math>a = -4; b = 3</math> (4 marks)</b> <ul style="list-style-type: none"> <li>•<sup>1</sup> uses synthetic division to find one equation</li> <li>•<sup>2</sup> uses synthetic division to find other eq.</li> <li>•<sup>3</sup> knows to use system of equations</li> <li>•<sup>4</sup> solves for <math>a</math> and <math>b</math></li> </ul>	<ul style="list-style-type: none"> <li>•<sup>1</sup> <math>b - a = 7</math></li> <li>•<sup>2</sup> <math>b + 3a = -9</math></li> <li>•<sup>3</sup> evidence</li> <li>•<sup>4</sup> <math>a = -4; b = 3</math></li> </ul>	

	Give 1 mark for each •	Illustration(s) for awarding each mark
13(a)	<p><b>ans: proof (3 marks)</b></p> <ul style="list-style-type: none"> <li>•<sup>1</sup> differentiates first term in brackets</li> <li>•<sup>2</sup> differentiates second term in brackets</li> <li>•<sup>3</sup> contracts <math>2\sin x \cos x</math> and simplifies</li> </ul>	<ul style="list-style-type: none"> <li>•<sup>1</sup> <math>\sqrt{3}(2\sin x \cos x \dots\dots)</math></li> <li>•<sup>2</sup> <math>\dots\dots 2\sin 2x</math></li> <li>•<sup>3</sup> <math>\sqrt{3}(\sin 2x + 2\sin 2x) = \sqrt{3}(3\sin 2x)</math></li> </ul>
(b)	<p><b>ans: 9/2 (2 marks)</b></p> <ul style="list-style-type: none"> <li>•<sup>1</sup> subs into derivative</li> <li>•<sup>2</sup> evaluates</li> </ul>	<ul style="list-style-type: none"> <li>•<sup>1</sup> <math>\sqrt{3}(3\sin 2(\frac{\pi}{6})); \sqrt{3}(3\sin \frac{\pi}{3})</math></li> <li>•<sup>2</sup> <math>\sqrt{3} \times 3 \times \frac{\sqrt{3}}{2} = \frac{9}{2}</math></li> </ul>
	<b>Sect. B (34 marks)</b>	<b>16 + 34 Total: 50 marks</b>